Panel Data

Difference in difference Interrupted time series Regression discontinuity Synthetic control

> lan Lundberg Soc 212B Winter 2025

5 Feb 2025

Learning goals for today

At the end of class, you will be able to:

- 1. Recognize the promises and pitfalls of four methods to study the effects of treatments that turn on once
 - 1.1 Difference in difference (DID)
 - 1.2 Interrupted time series (ITS)
 - 1.3 Regression discontinuity (RD)
 - 1.4 Synthetic control (SC)

Card, D., & Krueger, A. B. (1994). Minimum Wages and Employment: A Case Study of the Fast-Food Industry in New Jersey and Pennsylvania. The American Economic Review, 84(4), 772-793.

Economic theory

When the minimum wage rises, how might employment change?

Economic theory

When the minimum wage rises, how might employment change?

employees cost more

Economic theory

When the minimum wage rises, how might employment change?

- employees cost more
- employers might get by with fewer employees

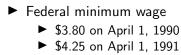
The setting

The setting



- ▶ \$3.80 on April 1, 1990
- ▶ \$4.25 on April 1, 1991

The setting



- New Jersey minimum wage
 - ▶ \$5.05 on April 1, 1992

NJ introduces a high minimum wage. How would you study the effect on employment? Source: Wikimedia

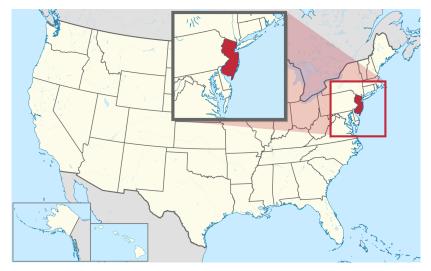




Photo by James Loesch - https://www.flickr.com/photos/jal33/49113053632/ CC BY 2.0, https://commons.wikimedia.org/w/index.php?curid=87207834

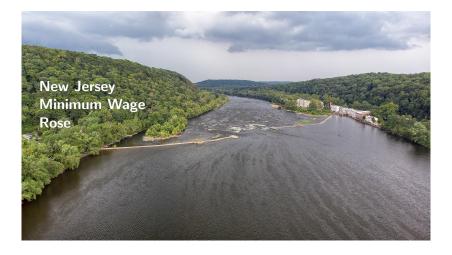


Photo by James Loesch - https://www.flickr.com/photos/jal33/49113053632/ CC BY 2.0, https://commons.wikimedia.org/w/index.php?curid=87207834



Photo by James Loesch - https://www.flickr.com/photos/jal33/49113053632/ CC BY 2.0, https://commons.wikimedia.org/w/index.php?curid=87207834







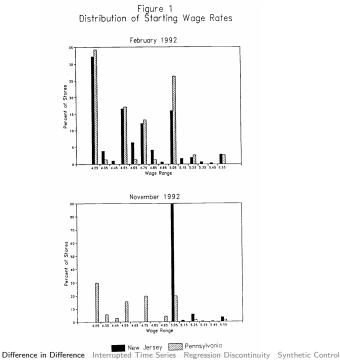
Phone interview: Feb-Mar 1992 before minimum wage rose Nov-Dec 1992 after minimum wage rose



Phone interview: Feb-Mar 1992 before minimum wage rose Nov-Dec 1992 after minimum wage rose

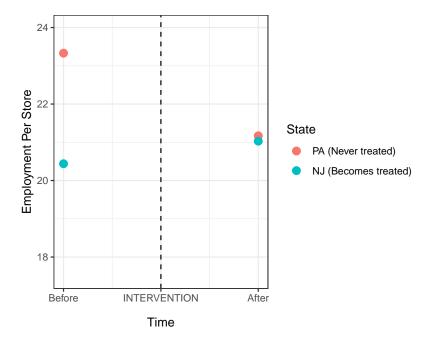
Recorded: How many full-time equivalent employees?

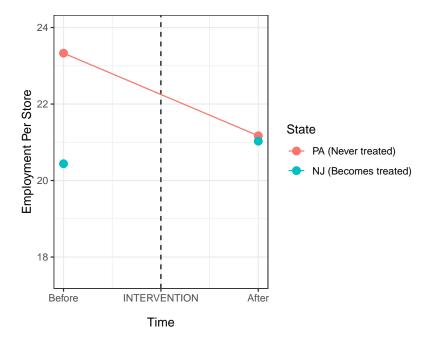
Did starting wages rise in NJ?

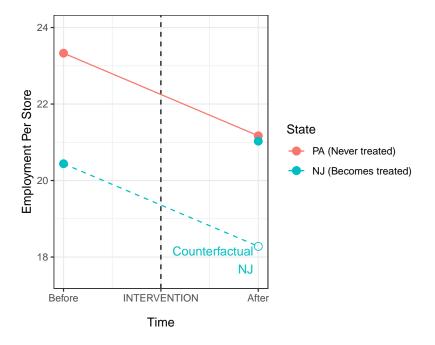


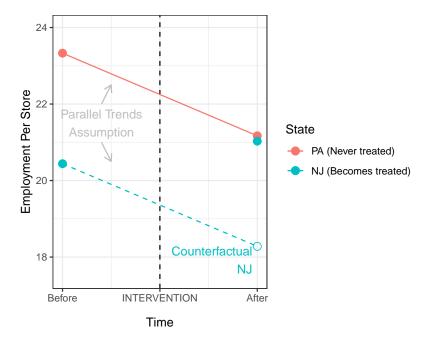
Panel Data

How did employment change?

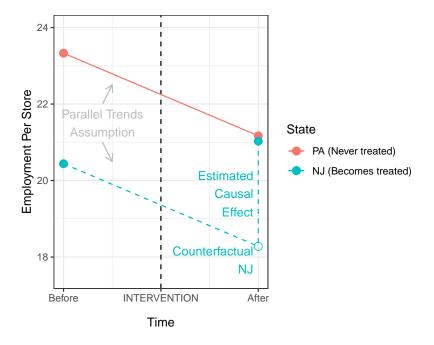








Panel Data Difference in Difference Interrupted Time Series Regression Discontinuity Synthetic Control



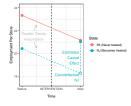
	Stores by state		
Variable	PA (i)	NJ (ii)	Difference, NJ-PA (iii)
1. FTE employment before, all available observations	23.33	20.44	-2.89
	(1.35)	(0.51)	(1.44)
2. FTE employment after,	21.17	21.03	-0.14
all available observations	(0.94)	(0.52)	(1.07)
3. Change in mean FTE employment	-2.16	0.59	2.76
	(1.25)	(0.54)	(1.36)

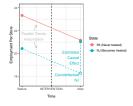
"Contrary to the central prediction of the textbook model of the minimum wage,...we find no evidence that the rise in New Jersey's minimum wage reduced employment at fast-food restaurants in the state."

Card & Krueger 1994, p. 792

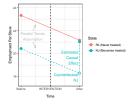
- ► simple study
- ► well-executed
- upended conventional wisdom

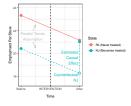
Key assumption: Parallel trends



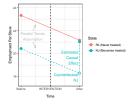


Parallel trends assumption:



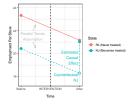


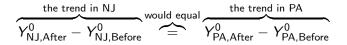




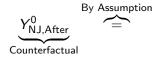


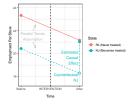
Rearranging yields a formula for the counterfactual outcome





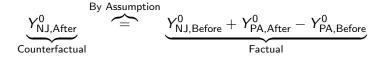
Rearranging yields a formula for the counterfactual outcome

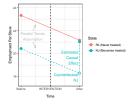




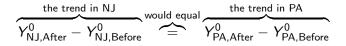


Rearranging yields a formula for the counterfactual outcome

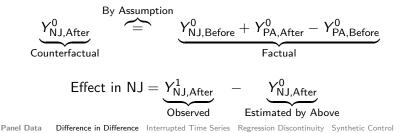




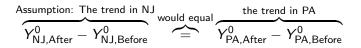
Parallel trends assumption: If no law had taken effect, then



Rearranging yields a formula for the counterfactual outcome

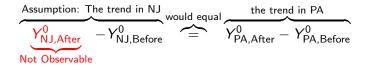


Can we test the parallel trends assumption?



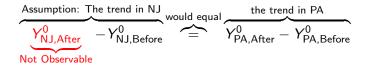
Can we test the parallel trends assumption?

No.



Can we test the parallel trends assumption?

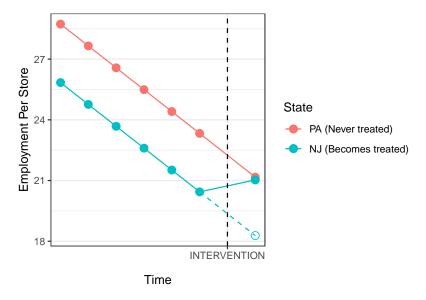
No.



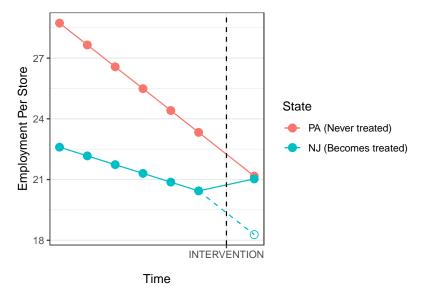
You can make it credible by looking at many pre-treatment periods

Panel Data Difference in Difference Interrupted Time Series Regression Discontinuity Synthetic Control

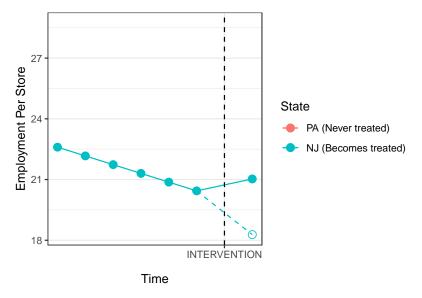
DID would be very credible



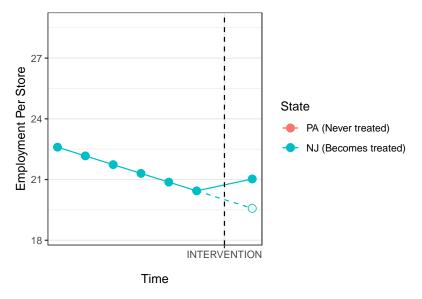
DID would be very doubtful



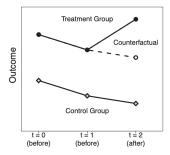
DID would be very doubtful

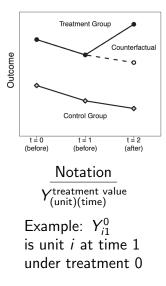


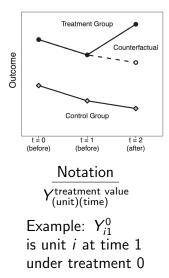
DID would be very doubtful



Egami, N., & Yamauchi, S. (2023). Using multiple pretreatment periods to improve difference-in-differences and staggered adoption designs. Political Analysis, 31(2), 195-212.

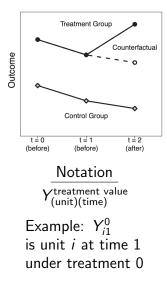






Parallel Trends Assumption (untestable)

$$E(Y^{0}_{\text{Treated},2} - Y^{0}_{\text{Treated},1}) = \\E(Y^{0}_{\text{Control},2} - Y^{0}_{\text{Control},1})$$

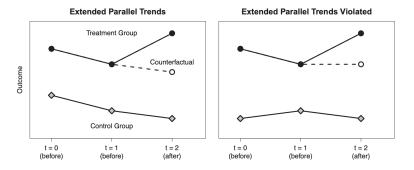


Parallel Trends Assumption (untestable)

$$E(Y^{0}_{\text{Treated},2} - Y^{0}_{\text{Treated},1}) = E(Y^{0}_{\text{Control},2} - Y^{0}_{\text{Control},1})$$

Extended Parallel Trends (testable)

$$E(Y^{0}_{\text{Treated},1} - Y^{0}_{\text{Treated},0}) = \\E(Y^{0}_{\text{Control},1} - Y^{0}_{\text{Control},0})$$

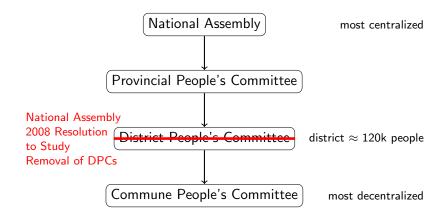


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Malesky, E. J., Nguyen, C. V., & Tran, A. (2014). The impact of recentralization on public services: A difference-in-differences analysis of the abolition of elected councils in Vietnam.

American Political Science Review, 108(1), 144-168.

Does government work better when it is centralized or decentralized?



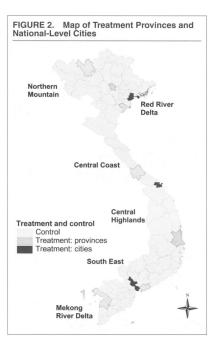
Input from social scientists

1. Enough treated units to study

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- 2. Sampling stratified by region

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- 2. Sampling stratified by region
- 3. Sampling stratified by
 - city versus rural
 - Iowland versus highland
 - midland versus inter-nationally bordered land

- 1. Enough treated units to study
- 2. Sampling stratified by region
- 3. Sampling stratified by
 - city versus rural
 - lowland versus highland
 - midland versus inter-nationally bordered land
- 4. Sampling stratified by socioeconomic and public administration performance



Panel Data Difference in Difference Interrupted Time Series Regression Discontinuity Synthetic Control

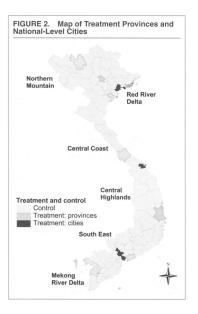
Vietnam Household Living Standards Survey Reports by each local commune by commune leaders

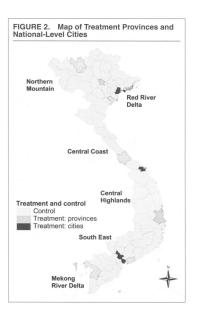
- ▶ 2006 and 2008: Before DPC abolition
- ► 2010: After DPC abolition

One outcome we will examine:

Is there the following project in the commune?

Investment on culture and education

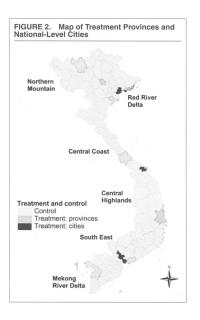




Outcome 1 Education and cultural programs

Is there the following project in the commune?

Investment on culture and education



Outcome 2 Tap water

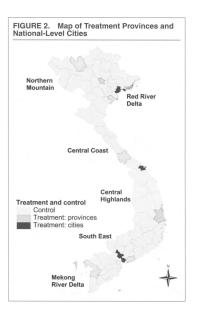
Is there the following project in the commune?

Coded 1

Indoor private piped water Outdoor private piped water Public piped water

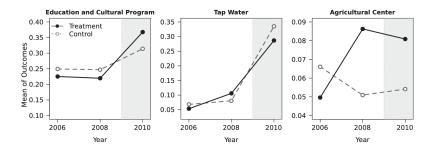
Coded 0

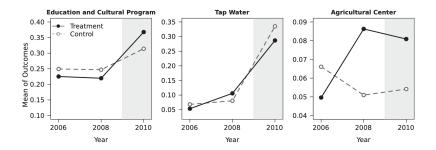
Well water Well with protection walls Well without protection walls Stream water with protection Stream water without protection Rainwater Bottled water Water brought by pedicab Tank water river lake pond



Outcome 3 Agricultural center

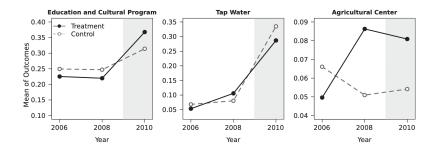
Is there any agriculture extension center in this commune?





In each case, do you believe parallel trends?

Panel Data Difference in Difference Interrupted Time Series Regression Discontinuity Synthetic Control



In each case, do you believe parallel trends?

Table 2. Assessing underlying assumptions using the pretreatment outcomes.

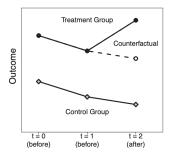
	Estimate	Std. error	<i>p</i> -value	95% Std. equivalence CI
Education and cultural program	-0.007	0.096	0.940	[-0.166,0.166]
Tap water	0.166	0.083	0.045	[-0.302,0.302]
Agricultural center	0.198	0.082	0.015	[-0.332,0.332]

Benefit 1: Assessing assumptions

Pre-treatment periods enable us to assess underlying ssumptions

Parallel trends is untestable, but being parallel in the pre-treatment period builds confidence

Pre-treatment periods also enable us to **improve estimation accuracy** when parallel trends holds

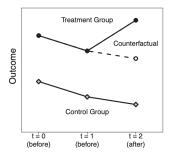


Estimator 1

Estimator 2

Notation

Ytreatment value (unit)(time)



Estimator 1

~

$$\underbrace{\left(\bar{Y}_{T2}^{1}-\bar{Y}_{T1}^{0}\right)}_{\left(\bar{Y}_{C2}^{0}-\bar{Y}_{C1}^{0}\right)}-\underbrace{\left(\bar{Y}_{C2}^{0}-\bar{Y}_{C1}^{0}\right)}_{\left(\bar{Y}_{C2}^{0}-\bar{Y}_{C1}^{0}\right)}$$

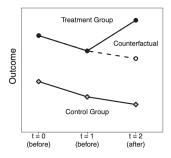
Treatment Group Time 2 - Time 1

Control Group Time 2 - Time 1

Estimator 2

Notation

Vtreatment value (unit)(time)



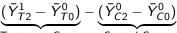
Estimator 1

$$\underbrace{\left(\bar{Y}_{T2}^{1}-\bar{Y}_{T1}^{0}\right)}_{\left(\bar{Y}_{C2}^{0}-\bar{Y}_{C1}^{0}\right)}-\underbrace{\left(\bar{Y}_{C2}^{0}-\bar{Y}_{C1}^{0}\right)}_{\left(\bar{Y}_{C2}^{0}-\bar{Y}_{C1}^{0}\right)}$$

Treatment Group Time 2 - Time 1

Control Group Time 2 - Time 1

Estimator 2



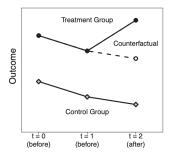
Treatment Group Time 2 - Time 0

Control Group Time 2 - Time 0

Notation

Y^{treatment value} (unit)(time)

Benefit 2: Improving efficiency



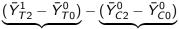
Estimator 1

$$\underbrace{\left(\bar{Y}_{T2}^{1}-\bar{Y}_{T1}^{0}\right)}_{\left(\bar{Y}_{C2}^{0}-\bar{Y}_{C1}^{0}\right)}-\underbrace{\left(\bar{Y}_{C2}^{0}-\bar{Y}_{C1}^{0}\right)}_{\left(\bar{Y}_{C2}^{0}-\bar{Y}_{C1}^{0}\right)}$$

Treatment Group Time 2 - Time 1

Control Group Time 2 - Time 1

Estimator 2





Treatment Group Time 2 - Time 0

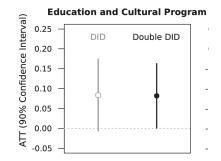
Control Group Time 2 - Time 0

Notation

✓treatment value (unit)(time)

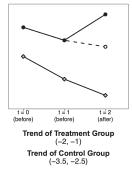
Pooled estimator: Average the two!

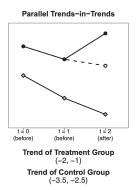
Benefit 2: Improving efficiency



Pre-treatment periods make it possible to allow for a more flexible parallel trends assumption

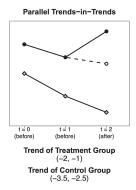






ASSUMPTION 3 (Parallel Trends-in-Trends)

$$\underbrace{\left\{ \mathbb{E}[Y_{l2}(0) \mid G_{i} = 1] - \mathbb{E}[Y_{l1}(0) \mid G_{i} = 1]\right\}}_{\text{Trend of the treatment group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 1] - \mathbb{E}[Y_{l0}(0) \mid G_{i} = 1]\right\}}_{\text{Trend of the control group from }t=0 \text{ to }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l2}(0) \mid G_{i} = 0] - \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0]\right\}}_{\text{Trend of the control group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] - \mathbb{E}[Y_{l0}(0) \mid G_{i} = 0]\right\}}_{\text{Trend of the control group from }t=0 \text{ to }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] - \mathbb{E}[Y_{l0}(0) \mid G_{i} = 0]\right\}}_{\text{Trend of the control group from }t=0 \text{ to }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] - \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0]\right\}}_{\text{Trend of the control group from }t=0 \text{ to }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] - \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0]\right\}}_{\text{Trend of the control group from }t=0 \text{ to }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] - \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0]\right\}}_{\text{Trend of the control group from }t=0 \text{ to }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] - \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0]\right\}}_{\text{Trend of the control group from }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] - \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] \right\}}_{\text{Trend of the control group from }t=0 \text{ to }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] - \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] \right\}}_{\text{Trend of the control group from }t=0 \text{ to }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] - \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] \right\}}_{\text{Trend of the control group from }t=0 \text{ to }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] - \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] \right\}}_{\text{Trend of the control group from }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] - \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] \right\}}_{\text{Trend of the control group from }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] - \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] \right\}}_{\text{Trend of the control group from }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] \right\}}_{\text{Trend of the control group from }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] \right\}}_{\text{Trend of the control group from }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] \right\}}_{\text{Trend of the control group from }t=1} \underbrace{\left\{ \mathbb{E}[Y_{l1}(0) \mid G_{i} = 0] \right\}}_{\text{Trend of the control group from }t=$$

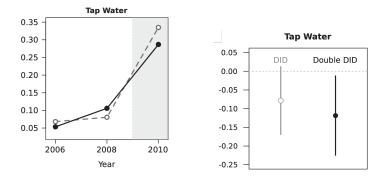


ASSUMPTION 3 (Parallel Trends-in-Trends)

$$\begin{split} \underbrace{\left\{ \mathbb{E}[Y_{12}(0) \mid G_i = 1] - \mathbb{E}[Y_{11}(0) \mid G_i = 1] \right\}}_{\text{Trend of the treatment group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 1] - \mathbb{E}[Y_{01}(0) \mid G_i = 1] \right\}}_{\text{Trend of the treatment group from }t=0 \text{ to }t=1} \\ = \underbrace{\left\{ \mathbb{E}[Y_{12}(0) \mid G_i = 0] - \mathbb{E}[Y_{11}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] - \mathbb{E}[Y_{01}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] - \mathbb{E}[Y_{01}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] - \mathbb{E}[Y_{01}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] - \mathbb{E}[Y_{01}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] - \mathbb{E}[Y_{01}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] - \mathbb{E}[Y_{01}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] - \mathbb{E}[Y_{01}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] - \mathbb{E}[Y_{01}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] - \mathbb{E}[Y_{11}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] - \mathbb{E}[Y_{11}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] - \mathbb{E}[Y_{11}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] - \mathbb{E}[Y_{11}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1 \text{ to }t=2} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1} \underbrace{\left\{ \mathbb{E}[Y_{11}(0) \mid G_i = 0] \right\}}_{\text{Trend of the control group from }t=1} \underbrace{\left\{$$

Sequential DID Estimator

$$\begin{split} \widehat{\tau}_{s-\text{DID}} &= \left\{ \left(\frac{\sum_{i:\ G_i=1} Y_{i2}}{n_{12}} - \frac{\sum_{i:\ G_i=1} Y_{i1}}{n_{11}} \right) - \left(\frac{\sum_{i:\ G_i=0} Y_{i2}}{n_{02}} - \frac{\sum_{i:\ G_i=0} Y_{i1}}{n_{01}} \right) \right\} \\ &- \left\{ \left(\frac{\sum_{i:\ G_i=1} Y_{i1}}{n_{11}} - \frac{\sum_{i:\ G_i=1} Y_{i0}}{n_{10}} \right) - \left(\frac{\sum_{i:\ G_i=0} Y_{i1}}{n_{01}} - \frac{\sum_{i:\ G_i=0} Y_{i0}}{n_{00}} \right) \right\}, \end{split}$$

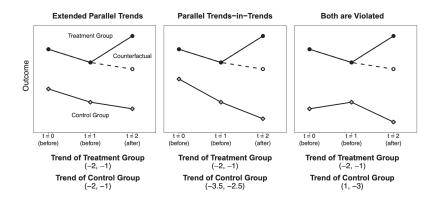


Benefits of multiple pre-treatment periods

- 1. assess underlying assumptions
- 2. improve estimation accuracy
- 3. allow for a more flexible parallel trends assumption

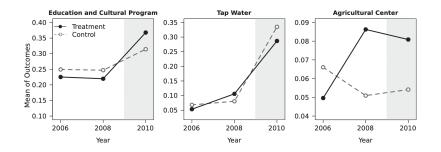
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Benefits of multiple pre-treatment periods

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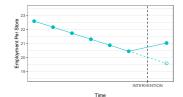


¹Bernal, J. L., Cummins, S., & Gasparrini, A. (2017). Interrupted time series regression for the evaluation of public health interventions: A tutorial. International Journal of Epidemiology, 46(1), 348-355.

You study one unit. It is untreated. Then it is treated.

¹Bernal, J. L., Cummins, S., & Gasparrini, A. (2017). Interrupted time series regression for the evaluation of public health interventions: A tutorial. International Journal of Epidemiology, 46(1), 348-355.

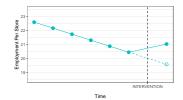
You study one unit. It is untreated. Then it is treated.



In what settings does this work well?

¹Bernal, J. L., Cummins, S., & Gasparrini, A. (2017). Interrupted time series regression for the evaluation of public health interventions: A tutorial. International Journal of Epidemiology, 46(1), 348-355. Panel Data Difference in Difference Interrupted Time Series Regression Discontinuity Synthetic Control

You study one unit. It is untreated. Then it is treated.

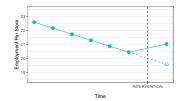


In what settings does this work well?

• When you have a strong pre-treatment trend to forecast Y_t^0

¹Bernal, J. L., Cummins, S., & Gasparrini, A. (2017). Interrupted time series regression for the evaluation of public health interventions: A tutorial. International Journal of Epidemiology, 46(1), 348-355. Panel Data Difference in Difference Interrupted Time Series Regression Discontinuity Synthetic Control

You study one unit. It is untreated. Then it is treated.

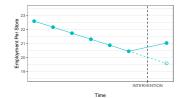


In what settings does this work well?

- When you have a strong pre-treatment trend to forecast Y_t^0
- When you don't have a comparable unit that is never treated

¹Bernal, J. L., Cummins, S., & Gasparrini, A. (2017). Interrupted time series regression for the evaluation of public health interventions: A tutorial. International Journal of Epidemiology, 46(1), 348-355. Panel Data Difference in Difference Interrupted Time Series Regression Discontinuity. Synthetic Control

You study one unit. It is untreated. Then it is treated.

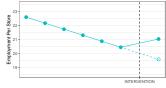


Theoretical Estimand

$$\mathsf{E}(Y^1-Y^0 \mid \mathcal{T} > t_{\mathsf{Intervention}})$$

¹Bernal, J. L., Cummins, S., & Gasparrini, A. (2017). Interrupted time series regression for the evaluation of publicshealths interventions such tutorial

You study one unit. It is untreated. Then it is treated.

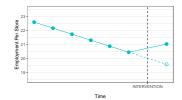


Time

Identifying Assumption

¹Bernal, J. L., Cummins, S., & Gasparrini, A. (2017). Interrupted time series regression for the evaluation of public health interventions: A tutorial. International Journal of Epidemiology, 46(1), 348-355. Panel Data Difference in Difference Interrupted Time Series Regression Discontinuity Synthetic Control

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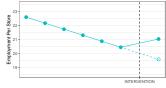


Identifying Assumption

In the absence of the intervention, the pre-intervention trend in Y⁰ would have continued

¹Bernal, J. L., Cummins, S., & Gasparrini, A. (2017). Interrupted time series regression for the evaluation of public health interventions: A tutorial. International Journal of Epidemiology, 46(1), 348-355. Panel Data Difference in Difference Interrupted Time Series Regression Discontinuity Synthetic Control

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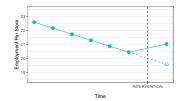


Time

Concrete steps:

¹Bernal, J. L., Cummins, S., & Gasparrini, A. (2017). Interrupted time series regression for the evaluation of public health interventions: A tutorial. International Journal of Epidemiology, 46(1), 348-355.

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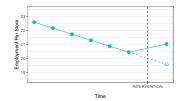


Concrete steps:

1. Learn a model on the pre-treatment period

¹Bernal, J. L., Cummins, S., & Gasparrini, A. (2017). Interrupted time series regression for the evaluation of public health interventions: A tutorial. International Journal of Epidemiology, 46(1), 348-355.

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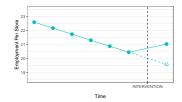


Concrete steps:

- 1. Learn a model on the pre-treatment period
 - Evaluation metric: Forecast within the pre-treatment period

¹Bernal, J. L., Cummins, S., & Gasparrini, A. (2017). Interrupted time series regression for the evaluation of public health interventions: A tutorial. International Journal of Epidemiology, 46(1), 348-355.

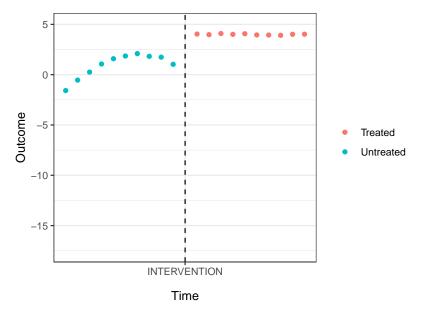
You study one unit. It is untreated. Then it is treated.

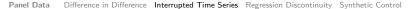


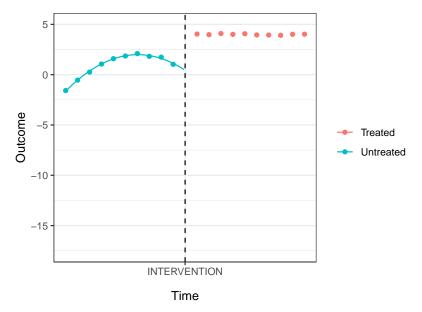
Concrete steps:

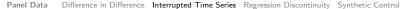
- 1. Learn a model on the pre-treatment period
 - Evaluation metric: Forecast within the pre-treatment period
- 2. Forecast Y^0 for the post-treatment period

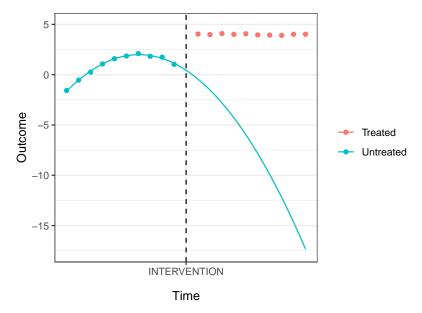
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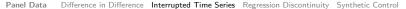


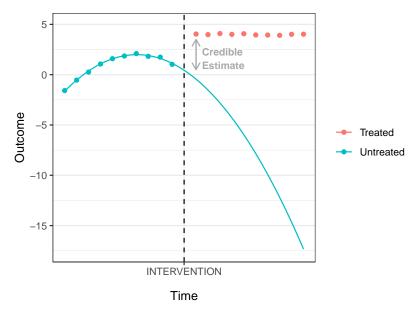




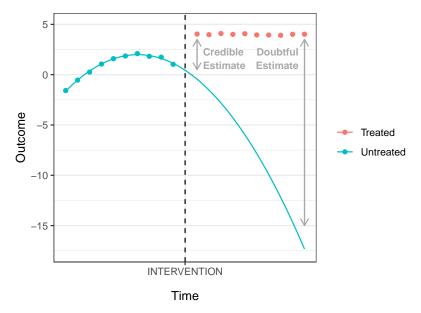














Interrupted time series: Recap

- ITS applies when treatment turns on at one time for all units
- ► ITS requires a parametric model to extrapolate
- ITS is most credible near the time when treatment turns on

When to use each method

► Difference in difference

- One unit becomes treated
- One unit never becomes treated
- ► The trends in Y⁰ are parallel

Interrupted time series

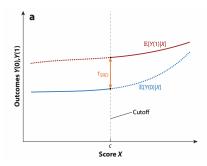
- Everyone becomes treated at X = c
- You believe you can forecast Y⁰ from X < c to X > c

New Jersey Pennsylvania

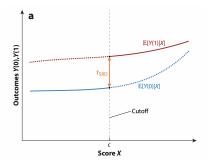
New drug Deaths would have been stable

²Cattaneo, M. D., & Titiunik, R. (2022). Regression discontinuity designs. Annual Reviewent Economics, 14, 821, 851, rise Regression Discontinuity Synthetic Control

Cattaneo & Titiunik 2022 Fig 1a



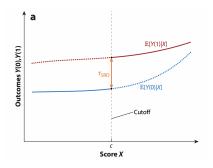
²Cattaneo, M. D., & Titiunik, R. (2022). Regression discontinuity designs. Annual Reviewent Economics, 14, 08217855 ries Regression Discontinuity Synthetic Control



Cattaneo & Titiunik 2022 Fig 1a

²Cattaneo, M. D., & Titiunik, R. (2022). Regression discontinuity designs. Annual Reviewent Economics, 14, 08217855 ries Regression Discontinuity Synthetic Control

Examples



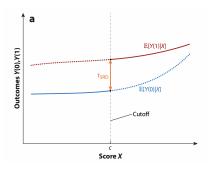
Cattaneo & Titiunik 2022 Fig 1a

Examples

X is PSAT test score c is a score cutoff A is National Merit Scholarship

(Thistlewaite & Campbell 1960)

²Cattaneo, M. D., & Titiunik, R. (2022). Regression discontinuity designs. Annual Reviewent Economics, 14, 0821, 895 ries Regression Discontinuity Synthetic Control



Cattaneo & Titiunik 2022 Fig 1a

Examples

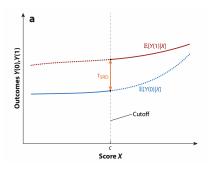
X is PSAT test score c is a score cutoff A is National Merit Scholarship

(Thistlewaite & Campbell 1960)

X is vote share c is 50% A is winning the election

(De la Cuesta & Imai 2016)

²Cattaneo, M. D., & Titiunik, R. (2022). Regression discontinuity designs. AnnualaReviewent Economics. 14, 821, 851, rise Regression Discontinuity Synthetic Control



Cattaneo & Titiunik 2022 Fig 1a

Examples

X is PSAT test score c is a score cutoff A is National Merit Scholarship

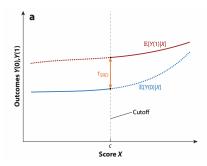
(Thistlewaite & Campbell 1960)

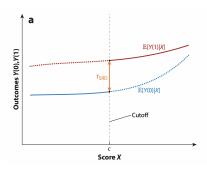
X is vote share c is 50%A is winning the election (De la Cuesta & Imai 2016)

X is date c is 2am Nov 6 2022 A is hours of PM darkness

²Cattaneo, M. D., & Titiunik, R. (2022). Regression discontinuity designs. AnnualaReviewent Economics, 14, 821, 854, riss Regression Discontinuity Synthetic Control

Cattaneo & Titiunik 2022 Fig 1a

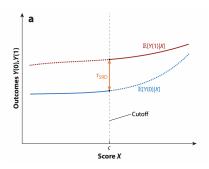




Cattaneo & Titiunik 2022 Fig 1a

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Theoretical Estimand E(Y(1) - Y(0) | X = c)

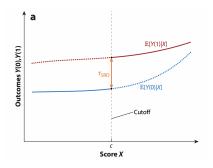


Cattaneo & Titiunik 2022 Fig 1a

Theoretical Estimand E(Y(1) - Y(0) | X = c)

Empirical Estimand $\lim_{x\downarrow c} E(Y \mid X = x)$

$$\lim_{x\uparrow c}\mathsf{E}(Y\mid X=x)$$



Cattaneo & Titiunik 2022 Fig 1a

Theoretical Estimand E(Y(1) - Y(0) | X = c)

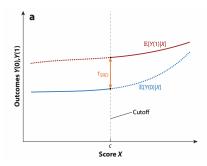
Empirical Estimand $\lim_{x\downarrow c} E(Y \mid X = x)$

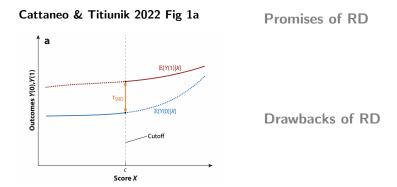
 $\lim_{x\uparrow c} \mathsf{E}(Y \mid X = x)$

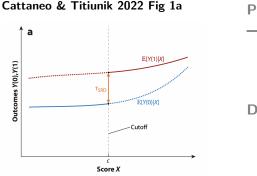
Identifying Assumptions E(Y(1) | X = x) and E(Y(0) | X = x) are continuous at x = c

and $f_X(x) > 0$ for x near c

Cattaneo & Titiunik 2022 Fig 1a

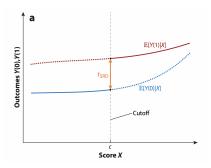






Promises of RD — Highly credible

Drawbacks of RD

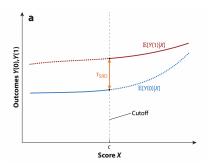


Cattaneo & Titiunik 2022 Fig 1a

Promises of RD

- Highly credible
- Easy to visualize

Drawbacks of RD

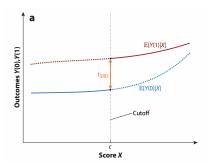


Cattaneo & Titiunik 2022 Fig 1a

Promises of RD

- Highly credible
- Easy to visualize

Drawbacks of RD — Local to X = c



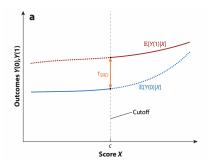
Cattaneo & Titiunik 2022 Fig 1a

Promises of RD

- Highly credible
- Easy to visualize

Drawbacks of RD

- Local to X = c
- Sensitive to sorting



Cattaneo & Titiunik 2022 Fig 1a

Promises of RD

- Highly credible
- Easy to visualize

Drawbacks of RD

- Local to X = c
- Sensitive to sorting

(people moving strategically over the cutoff)

When to use each method

 Difference in difference One unit becomes treated One unit never becomes treated The trends in Y⁰ are parallel 	New Jersey Pennsylvania
 Interrupted time series Everyone becomes treated at X = c You believe you can forecast Y⁰ from X < c to X > c 	New drug Deaths would have been stable
 Regression discontinuity 	
• Everyone becomes treated at $X = c$	Win the election
 You want a local estimate E(Y¹ − Y⁰ X = c) at the cutoff Y⁰ and Y¹ are continuous at X = c 	Close elections

³Abadie, A., Diamond, A., & Hainmueller, J. (2010). Synthetic control methods for comparative case studies: Estimating the effect of California's tobacco control program. Journal of the American Statistical Association, 105(490), 493-505.

In 1988, California implemented a tobacco control program

³Abadie, A., Diamond, A., & Hainmueller, J. (2010). Synthetic control methods for comparative case studies: Estimating the effect of California's tobacco control program. Journal of the American Statistical Association, 105(490), 493-505.

In 1988, California implemented a tobacco control program

New tax: 25 cents per pack

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In 1988, California implemented a tobacco control program

- ► New tax: 25 cents per pack
- Money earmarked for smoking-reduction programs

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In 1988, California implemented a tobacco control program

- ► New tax: 25 cents per pack
- Money earmarked for smoking-reduction programs

How much did it reduce CA cigarette sales in 1990? 1995? 2000?

³Abadie, A., Diamond, A., & Hainmueller, J. (2010). Synthetic control methods for comparative case studies: Estimating the effect of California's tobacco control program. Journal of the American Statistical Association, 105(490), 493-505.

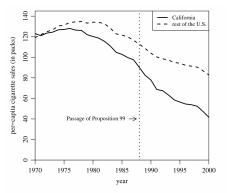


Figure 1. Trends in per-capita cigarette sales: California vs. the rest of the United States.

Can't use RD — Effect at 1988 not of interest

Can't use ITS

— Hard to extrapolate Y^0 trend

Can't use DID — No other state like CA

Idea: Create a synthetic CA to estimate $Y^0_{CA,t}$ for $t \ge 1988$

⁴Abadie, A., Diamond, A., & Hainmueller, J. (2010). Synthetic control methods for comparative case studies: Estimating the effect of California's tobacco control program. Journal of the American Statistical Association, 105(490), 493-505.

Synthetic CA as a weighted average of other states

	California		
Variables	Real	Synthetic	Average of 38 control states
Ln(GDP per capita)	10.08	9.86	9.86
Percent aged 15-24	17.40	17.40	17.29
Retail price	89.42	89.41	87.27
Beer consumption per capita	24.28	24.20	23.75
Cigarette sales per capita 1988	90.10	91.62	114.20
Cigarette sales per capita 1980	120.20	120.43	136.58
Cigarette sales per capita 1975	127.10	126.99	132.81

Table 1. Cigarette sales predictor means

NOTE: All variables except lagged cigarette sales are averaged for the 1980–1988 period (beer consumption is averaged 1984–1988). GDP per capita is measured in 1997 dollars, retail prices are measured in cents, beer consumption is measured in gallons, and cigarette sales are measured in packs.

⁵Abadie, A., Diamond, A., & Hainmueller, J. (2010). Synthetic control methods for comparative case studies: Estimating the effect of California's tobacco control program. Journal of the American Statistical Association, 105(490), 493-505.

Synthetic CA as a weighted average of other states

Theoretical Estimand:
$$au(t) = Y^1_{\mathsf{CA},t} - Y^0_{\mathsf{CA},t}$$
 $t \geq 1988$

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Synthetic CA as a weighted average of other states

Theoretical Estimand:
$$au(t)=Y^1_{\mathsf{CA},t}-Y^0_{\mathsf{CA},t}$$
 $t\geq 1988$

Empirical Estimand: $\theta(t) = Y_{CA,t}^1 - Y_{SyntheticCA,t}^0$ $t \ge 1988$

⁶Abadie, A., Diamond, A., & Hainmueller, J. (2010). Synthetic control methods for comparative case studies: Estimating the effect of California's tobacco control program. Journal of the American Statistical Association, 105(490), 493-505.

Synthetic CA as a weighted average of other states

⁶Abadie, A., Diamond, A., & Hainmueller, J. (2010). Synthetic control methods for comparative case studies: Estimating the effect of California's tobacco control program. Journal of the American Statistical Association, 105(490), 493-505.

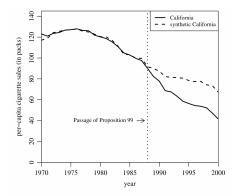


Figure 2. Trends in per-capita cigarette sales: California vs. synthetic California.

⁷Abadie, A., Diamond, A., & Hainmueller, J. (2010). Synthetic control methods for comparative case studies: Estimating the effect of California's tobacco control program. Journal of the American Statistical Association, 105(490), 493-505.

When to use each method

New Jersey
Pennsylvania
New drug
Deaths would
have been stable
Win the election
Close elections
California
Other states
$1988 { ightarrow} 2000$

Discussion

- What data do you need to use the method?
- ► What are the most likely limitations?
- How would you generalize your method to settings where many units become treated, potentially at different time points (staggered adoption)?

Learning goals for today

At the end of class, you will be able to:

- 1. Recognize the promises and pitfalls of four methods to study the effects of treatments that turn on once
 - 1.1 Difference in difference (DID)
 - 1.2 Interrupted time series (ITS)
 - 1.3 Regression discontinuity (RD)
 - 1.4 Synthetic control (SC)